ECON 712A: Macroeconomic Theory

Discussion Section Handout 1

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• Icebreaker: Names, pronouns, program, year, and field(s) of interest.

Administrative Information

- Teaching Assistants:
 - Duong Dang (dqdang@wisc.edu; 6439 Social Science; 3rd year)
 - Alex von Hafften (vonhafften@wisc.edu; 6473 Social Science; 2nd year).
- Weekly Schedule:
 - Monday: Lecture at 1:00 2:15 PM in 4028 Vilas.
 - Tuesday: Duong's office hours at 10:30 AM 11:45 PM in 6439 Social Science.
 - Wednesday: Lecture at 1:00 2:15 PM in 4028 Vilas.
 - Thursday:
 - * Discussion section handout and next problem set distributed.
 - $\ast\,$ Dean's office hours at 10:00 11:45 AM in 7438 Social Sciences.
 - $\ast\,$ Alex's office hours at 2:15 PM 3:30 PM in 6473 Social Science.
 - * Problem set due at 11:59 PM. Everyone needs to submit the problem set. Include a note about who you worked with.
 - Friday:
 - * Discussion sections
 - * Distribute discussion sections handout with solutions.
- Midterm on November 1 at 7:15 PM.
- Course Materials:
 - Everything will be posted on Canvas.
 - Lecture notes and past midterms are also available at https://sites.google.com/a/wisc.edu/ deancorbae/teaching.
 - Problem sets and section handouts are also available at https://vonhafften.github.io/teaching.html.
 - Problem sets will include computational problems. Any programming language will be accepted. Use the language that you're most comfortable with.
 - Example code will be provided largely in Matlab, Python, Julia, and/or R.

- Matlab is available at https://it.wisc.edu/services/software/.
- Ljungqvist and Sargent (textbook) is available online at the UW Madison Library.
- Discussion Sections:
 - 7:45 AM section is in 6105 Social Science.
 - 8:50 AM section is in 214 Ingraham
 - 2:25 PM section is in 6109 Social Science.
 - 3:30 PM section is in 6109 Social Science.
 - Sections are 50 minutes long.
 - Duong and Alex will alternate teaching all four sections each week.
- COVID Policies:
 - Masks covering your nose and mouth are required regardless of vaccination status.
 - To keep room capacity under control, please attend the section that you're enrolled in.
- What's the point of discussion sections?
 - Solving problems using concepts from lectures.
 - Filling in material omitted from lectures due to time constraints.
 - Discussing common issues on problem sets.
- Recommendations:
 - Study in groups.
 - Engage in active learning. Do practice problems.
 - Keep a positive mindset.
 - Recommendations for us? Email or anonymous feedback form at https://vonhafften.github.io/ teaching.html.

Content Review

- An **environment** is a statement of population, preferences, and technologies (e.g., production, matching, information, commitment).
- Example: An overlapping generation economy with endowments and log preferences.
 - Population: 2-period lived agents.
 - Production: Non-storable w_1 for young agents and 0 for old agents.
 - Preference: $U(c_t^t, c_{t+1}^t) = \ln(c_t^t) + \ln(c_{t+1}^t)$
- An allocation is a statement about how resources are distributed.
- If an allocation can be achieved given technologies, the allocation is resource feasible.

$$c_t^t + c_t^{t-1} \le w_1$$

• The **planner** allocates resources optimally given feasibility.

• What does optimally mean? So far, the planner has equally weighed the utility of each generation alive at period t:¹

$$\max_{\substack{c_t^t, c_t^{t-1} \in \mathbb{R}^2_+ \\ \text{s.t. } c_t^t + c_t^{t-1} \le w_1}} \ln(c_t^t) + \ln(c_t^{t-1})$$

• If the resource constraint holds with equality, we can use **substitution** to modify the planner problem into an unconstrained optimization problem.

$$\max_{c_t^t \in \mathbb{R}_+} \ln(c_t^t) + \ln(w_1 - c_t^t)$$

• The first order condition implies:

$$\implies c_t^t = c_t^{t-1} = \frac{w_1}{2}$$

- Planner problem is much better than **autarky**, in which agents only consume their endowments.
- How to **decentralize** the planner solution?
- One way is with **fiat currency**. The government issues M units of currency to the initial old.
- Taking p_1 as given, the problem of the initial old agents:

$$\max_{\substack{c_1^0 \in R_+ \\ \text{s.t. } p_1 c_1^0 \le M}} \ln(c_1^0)$$

$$\implies c_1^0 = M/p_1$$

- Let M_{t+1}^t be the flat currency holding of generation t to period t+1.
- Taking p_t, p_{t+1} as given, the problem of agents in all generations born in $t \ge 1$:

$$\begin{split} \max_{\substack{(c_t^t, c_{t+1}^t, M_{t+1}^t) \in \mathbb{R}_+^3 \\ \text{s.t. } p_t c_t^t + M_{t+1}^t = p_t w_1 \\ p_{t+1} c_{t+1}^t = M_{t+1}^t \end{split}}$$

$$\implies M_{t+1}^t = \frac{p_t w_1}{2}$$
$$c_t^t = \frac{w_1}{2}$$
$$c_{t+1}^t = \frac{p_t}{p_{t+1}} \frac{w_1}{2}$$

• Any questions?

 $^{^1\}mathrm{To}$ be specific, this planner problem is a *period-by-period utilitarian planner problem*

Growing and Shrinking Populations

Consider the baseline 2-period overlapping-generation model outlined in lecture but the population changes each generation. In particular, if there is N_t measure of generation t, then there is $N_{t+1} = nN_t$ of generation t+1 where $n \in \mathbb{R}_+$. Notice that population could be shrinking (0 < n < 1), staying the same (n = 1), or growing (n > 1).

- 1. What is the resource constraint with the changing population?
- 2. Is the planners allocation without population growth (i.e., $c_t^t = c_t^{t-1} = \frac{w_1}{2}$) resource feasible for a growing population? For a shrinking population?
- 3. The planner cares equally about all agents alive at period t. What is the planners problem?
- 4. What is the planners allocation?
- 5. Consider decentralizing the planner solution. How should we design a lump-sum tax and transfer system would achieve the planner solution?
- 6. Would agents prefer to live in an economy with a growing population or a shrinking population?

Pareto Weights

So far, we've consider a planner than weights agents equally, but we can consider optimal allocations where the planner applies different weights to different agents. These weights are referred to as "Pareto weights."

- 1. Consider the baseline overlapping generations model with 2-period lived agents without population growth. Setup a planner problem where young agents have weight λ_1 and old agents have weight λ_2 .
- 2. Solve for the optimal allocation a function of w_1 , λ_1 , and λ_2 .
- 3. Set $\lambda_2 = 1 \lambda_1$. How does the optimal allocation change for $\lambda_1 \in [0, 1]$?